



## Research Article

# Flow of viscous nanofluids across a non-linear stretching sheet

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## ABSTRACT

This article aims to demonstrate the flow of viscous nanofluid over a non-linear stretching sheet. Considering thermal radiation and dissipative heat in the heat transport phenomenon encourages the flow properties. In generally, nanofluids are employed in heat transfer equipment because they improve the thermal characteristics of coolants present in the equipment. Additionally, these fluids possess unique features that have the potential to be applied in a variety of applications, such as pharmaceutical procedures, hybrid power engines, household refrigerators, grinding, and microchips, among others. Consequently, the current model is built to allow for the optimal selection of thermophysical parameters such as conductivity and viscosity, which will enhance the overall effectiveness of the study. Appropriate transformation rules have been used to modify the highly non-linear PDEs into a couple of highly non-linear ODEs. An efficient built-in MATLAB bvp5c algorithm addresses the boundary value problem under consideration. Using the dimensionless parameters assumed in the problem, changes in the velocity as well as the temperature profiles are shown, and rate coefficients, by using numerical simulations are also employed in tabular form. The important outcomes which are exposed in the study are; that the particle concentration is used as a controlling parameter to reduce the nanofluid velocity, whereas it favours enhancing the fluid temperature and the radiating heat along with the coupling parameter due to the inclusion of dissipative heat also encourages to overshoot the temperature profile.

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## INTRODUCTION

The mass production, technical, and industrial range of various devices is supported by the research of many scientists and researchers. Timers are used in several industrial

devices lower their heat capacity. Researchers have explored a variety of lubricants to see if they may help prevent these issues and keep the temperature inside the device stable. But, the heat storage capacity of these pure liquids is

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insufficient for industrial use. The concept of nanofluids has arisen as a result of this. This paper includes a detailed nanofluid model that is intimate. Choi and Eastman [1] sought to test copper water in numerous experimental facilities utilizing pure nanofluids that had improved heat capacity compared to pure liquids, but their experiments were unsuccessful. Rashad et al. [2] examined laminar flow and continuous boundary layer nanofluid flow on a vertical cylinder through a porous medium. As detailed in this work, several associated factors were tested using excellent parametric tests. Ramreddy et al. [3] researched the conductivity of conductive nanofluids flowing over a flat plate. El-Kabeim et al. [4] conducted yet another investigation into the effects of non-administered porous media, heat radiation, and Forchheimer terms on the body. Lin et al. [5] employed Carboxy Methyl Cellulose water with four distinct nanoparticles as the basic solution, then diluted it with water. Mesoporous fluid particles are included in this category, with the deformation of microporous fluid particles being ignored. Many of the flow properties were reproduced in this model. Mishra et al. [6] and Bakar et al. [7] have investigated MHD's natural and forced convection.

The Maxwell model is used to determine which model of the behavior of non-Newtonian fluids is the most accurate. Madhu et al. [8] emphasize the flow of unsteady laminar MHD-Maxwell nanofluids with non-uniform velocities and non-uniform magnetic fields and the flow of unsteady laminar MHD-Maxwell nanofluids with non-uniform magnetic fields. According to Mishra et al. [9], the analysis of viscoelastic fluids' mass and heat transfer was carried out while considering chemical processes and external heating. This problem, known as the von Kalman problem, is employed for infinitely rotating discs in which conductive nanofluids serve as the disc's structural constituents (see [10]). With the help of a Williamson fluid, Qayyum et al. [11] demonstrate the creation of entropy between two rotating discs. In their research, Afridi and Kasim [12] investigated entropy creation by fine needles moving in the centre of parallel currents. The consequences of thermal radiation parameter and dissipation factors are emphasized in this piece of work. Khan et al. [13] investigated a two-dimensional lateral liquid flow that grows toward the blade when the chemical reaction concentration is kept constant. As a result of the originality of the research, the temperature equation now includes a discussion of the impact of heat radiation on heat generation/absorption. A new flow model for nanomaterials has been developed ([14]). In the given paper, Williamson fluids are used to formulate the problem. A numerical study of the flow of viscous and nano liquids on an expanding surface has been carried out by Jena and her co-researchers [15-17]. Magnetic and radiative effects on the water-alumina nanofluids using numerical simulations have been carried out by Sheikholeslami et al. [18].

The application of thermal radiation is useful in various medical treatments like cancer therapy, radiotherapy,

blockage removal from arteries, etc. Further, non-Newtonian nanofluid became popular in various oil industries plastic industries because of the high thermal conductivity of the nanoparticle.

The concept of magnetohydrodynamics (MHD) is introduced, which interacts with conductive fluids and magnetic fields in fluid flow to produce a fluid flow. The heat transfer characteristics of the fluid flow system are improved as a result of this procedure. Numerous theoretical, computational, and analytical research [19-21] have been carried out on different nanofluids (MHD) for distinct parametric effects, with the results being compared. Jena et al. [22] made significant contributions to investigating chemical reaction heat transmission in nanofluids and developing mathematical models of porous matrices. Acharya et al. [23] investigated the impacts of thermal energy on viscous fluids by using analytical calculations to theoretically assess the effects of thermal energy. According to several assessments, nanotechnology presents a platform suitable for ultrahigh coolant crises. Tshivhi and Makinde studied the use of nanofluids as coolants in MHDs in which the nanofluid flows over heated contraction/elongation surfaces [24]. Elsaid [25, 26], in a study combining wet cooling towers and vapor compression air conditioning systems, included his  $\text{Co}_3\text{O}_4$ -based and his  $\text{Al}_2\text{O}_3$ -based  $\text{H}_2\text{O}/(\text{CH}_2\text{OH})_2$  nanofluids in vehicle engine radiators. indicated that Friction coefficients were estimated and used for MgO and TiO<sub>2</sub>. to the base  $\text{H}_2\text{O}$  nanofluid. Elsaid et al. [27, 28] conducted an exergy analysis on various perforated rib designs utilised in triple tubes heat transfers that used hybrid nanofluids as well as various single and hybrid nanofluids in chilled water to test the stability of air conditioning systems. To make nanofluids better, some more interesting studies [29-31] have been done, which have been considered in the current situation. Hakeem and his coresearchers [32-35] have made a healthy contribution to the field of MHD nanofluid and hybrid nanofluid flow over a stretching sheet.

### Formulation of the problem

This article will consider the 2D steady flow of viscous incompressible nanofluids that pass through a non-linearly stretchable surface. Two equally opposite forces constrain the flow near the collapsing plate. The stretching speed of the sheet is  $\tilde{u}_w(x) = cx^n$  c, a constant realized by fixing the origin. At the same time,  $\tilde{T}_w(x) = T_\infty + bx^m$  is the temperature,  $\tilde{T}_w$  wall temperature, and  $T_\infty$ , ambient temperature were kept on the wall. The coordinate system's physical model (Figure 1) has been followed. The basic equations, i.e., the equation of mass, the equation of momentum, and the energy equation for nanofluids using the general boundary layer approximation, have been considered. Earlier published work [36] is converted to a nanofluid model:

$$\tilde{u}\tilde{u}_x + \tilde{v}\tilde{u}_y = \nu_{nf}\tilde{u}_{yy}$$

$$\tilde{u}_x + \tilde{v}_y = 0,$$

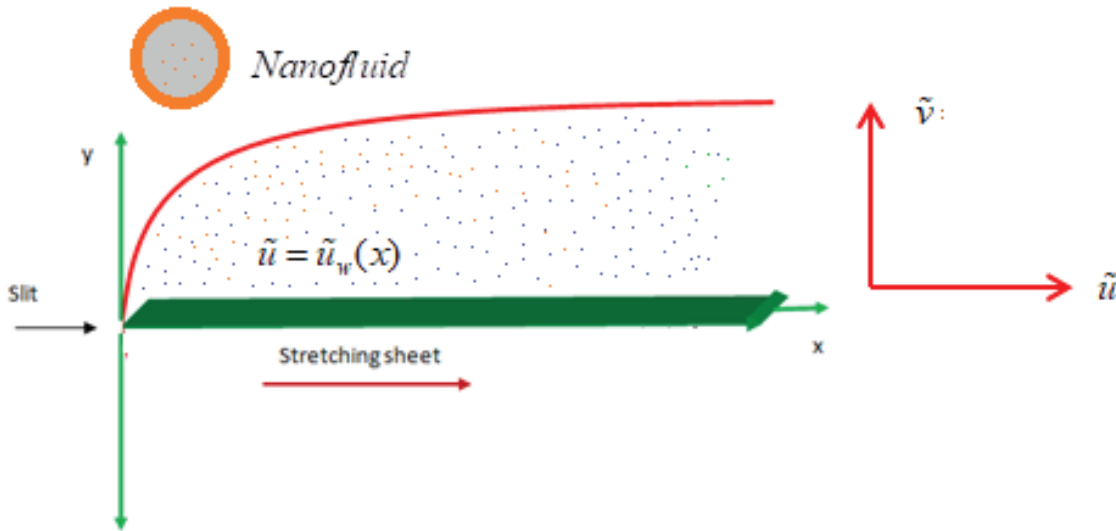


Figure 1. Hemisphere shows the direction of incident radiation and solid angle relations [16].

Equation of Continuity:

$$\tilde{u}_x + \tilde{v}_y = 0,$$

(1)

$$\mu_{nf} = \mu_f (1 - \phi)^{-2.5}, \quad \frac{k_{nf}}{k_f} = \frac{(\Omega + 2) - 2\phi(1 - \Omega)}{(\Omega + 2) + \phi(1 - \Omega)}, \quad \Omega = \frac{k_s}{k_f},$$

$$\frac{\rho_{nf}}{\rho_f} = 1 - \phi + \frac{\rho_s}{\rho_f}, \quad \frac{(\rho c_p)_{nf}}{(\rho c_p)_f} = 1 - \phi + \phi \frac{(\rho c_p)_s}{(\rho c_p)_f}.$$

(7)

Equation of Momentum:

$$\tilde{u}\tilde{u}_x + \tilde{v}\tilde{u}_y = \nu_{nf}\tilde{u}_{yy}$$

(2)

Radiative heat flux (Rosseland approximation) is ([37]):

$$q_r = -\frac{4\sigma^*}{3k^*} [\tilde{T}^4]_y$$

(3)

Equation of Energy:

Expansion of  $\tilde{T}^4$  by the Taylor series method we have (neglecting higher order terms),

$$\tilde{u}\tilde{T}_x + \tilde{v}\tilde{T}_y = \frac{k_{nf}}{(\rho c_p)_{nf}} \tilde{T}_{yy} + \frac{\mu_{nf}}{(\rho c_p)_{nf}} \tilde{u}_y^2 - \frac{1}{(\rho c_p)_{nf}} (q_r)_y$$

(4)

$$\tilde{T}^4 \cong 4\tilde{T}_\infty^3 - 3\tilde{T}_\infty^4$$

Introduction of non-dimensional variables ( $m = 2n$ ):

$$\eta = yx^{\frac{n+1}{2}} \sqrt{\frac{n+1}{\mu_f}} \sqrt{\frac{c}{2}}, \quad \tilde{u} = cx^\alpha f', \quad \tilde{v} = -\sqrt{c(n+1)} \sqrt{\frac{\mu_f}{2}} \left( f - \eta \frac{n-1}{n+1} f' \right) x^{\frac{n-1}{2}}, \quad \tilde{T} = T_\infty + (T_w - T_\infty) \theta(\eta).$$

(5)

For,  $y = 0$ ,  $\tilde{u} = \tilde{u}_w(x)$ ,  $\tilde{v} = 0$ , and  $\tilde{T} = T_w(x)$

causes,

when,  $y \rightarrow \infty$ ,  $\tilde{u} \rightarrow 0$  and  $\tilde{T} \rightarrow T_\infty$

(6)

$$\frac{1}{A} f''' - \frac{2n}{n+1} f'^2 + ff'' = 0$$

(10)

The density and effective viscosity (see [17]) of the nanofluid are defined as,

$$\frac{1}{\text{Pr} B} \left( \frac{k_{nf}}{k_f} + Nr \right) \theta'' + f\theta' - \frac{4n}{n+1} f'\theta + \frac{A_1}{B} Ec f''^2 = 0$$

(11)

for  $\eta = 0, f = 0, f' = 1$ , and  $\theta(0) = 1$

$$\text{when } \eta \rightarrow \infty, f' \rightarrow 0, \text{ and } \theta \rightarrow 0. \quad (12)$$

where,

$$\left. \begin{aligned} A &= (1-\phi)^{2.5} \left( 1-\phi + \frac{\rho_s}{\rho_f} \phi \right), B = 1-\phi + \frac{(\rho c_p)_s}{(\rho c_p)_f} \phi, \\ \text{Pr} &= \frac{\mu_f}{\alpha_f}, \text{Nr} = \frac{16k^*}{3\sigma^* T_\infty^3}, \text{Ec} = \frac{\tilde{u}_w}{(\rho c_p)_f (T_w - T_\infty)} \end{aligned} \right\} \quad (13)$$

For , Eqns. (9) & (11) gave classical Blasius flat-plate flow problem (see [38]). For (linear stretching), the unique solution of Eqn. (9) can be , whereas there is no exact solution with (non-linearly stretching).

### Physical quantities of practical interest

We have studied the skin friction coefficient ( $C_f$ ) and the local Nusselt number ( $N_u$ ), which can be defined as:

$$C_f = \frac{\mu_{nf}}{\rho_f} \frac{2}{\tilde{u}_w^2(x)} \left[ \tilde{u}_y \right]_{y=0}, Nu = -\frac{k_{nf}}{k_f} \frac{x}{(T_w - T_\infty)} \left[ \tilde{T}_y \right]_{y=0}. \quad (14)$$

Putting Eqn. (9) in Eqn. (12), one can get:

$$\sqrt{\frac{c}{2}} \frac{x^{n+1}}{\mu_f} C_f = \sqrt{n+1} \frac{f''(0)}{(1-\phi)^{-5/2}}, Nu \sqrt{\frac{\mu_f}{c}} \sqrt{\frac{2}{x^{n+1}}} = -\sqrt{n+1} \left( \frac{k_{nf}}{k_f} + \text{Nr} \right) \theta'(0). \quad (15)$$

## DISCUSSIONS OF RESULT

The two-dimensional flow of nanofluid over a non-linearly stretching sheet is presented in the current analysis. The role of radiative heat and dissipative heat enriches the flow phenomena. The proposed design model is handled numerically using a suitable built-in MATLAB code bvp5c. Table 1 shows the physical properties of the base fluid (water and Kerosene) and nanoparticle (Copper). Table 2 shows the simulated results of rate coefficients for both the Water and Kerosene-based nanofluids, and these are in good agreement with previous studies of Khan and Pop [39] and Devi and Devi [40]. This can be evident from the numerical calculations of  $f$  and  $Nu$ .

Further, Table 3 exhibits the numerical results of and for the different restriction values in Water and Kerosene-based nanofluids. In addition, the increase in volume fraction parameter ( $\phi$ ), enhances the  $C_f$  and  $N_u$ . However, the results using Kerosene-based nanofluids dominate over Water-based nanofluids. The non-linear strain parameter ( $n$ ) reduces but reverses the for both the nanofluids. The Prandtl number increases the Nusselt number, but the radiation parameter and Eckert number have an opposite impact.

Further, a t-test for the skin friction data and the Nusselt number is presented for a confidence level of 95%. The

hypothetical test assuming the null mean was rejected for both cases. The results are presented in Table 4. This reveals that the parametric behaviour obtained by the numerically simulated result for the diversified values of the parameters is valid data that will validate the present study. Moreover, a correlation coefficient is calculated with their variances and presented thereat for the paired two-sample mean. Besides that, the computations are obtained numerically and discussed graphically, assuming the assigned values of the parameters, except for the specific variations of the parameter in the corresponding graph.

Figure 2 compares the Cu~Water and Cu~Kerosene nanofluids for the variation of volume fraction ( $\phi$ ) on the velocity profile. The flow phenomena are characterized by the thermophysical properties that depend on particle concentration. Therefore the role of particle concentration is vital. It is the amount of dispersion of the solid particles into the base liquid. It is evident that enhanced volume fraction ( $\phi$ ) leads to decelerating the velocity distribution because of the heavier density of the solid particles. In a comparative analysis, it is seen that the retardation in the case of Cu~Kerosene is slower than that of Cu~Water because the density of the transported water is slower than that of Kerosene. Figure 3 shows the effect of on the temperature profile considering both the base fluids. When it increases, a slight change will occur. i.e., the profile will increase with increasing . It occurs due to the variation described in an earlier result that particle concentration retards the velocity, and that is the reason the clogging of the particles generates energy near the surface region, and the stored energy gives rise to overshooting the profile, and therefore, the fluid temperature increases significantly. Finally, it is concluded that the magnitude in the case of a Water-based nanofluid is higher than that of a kerosene-based nanofluid. Figures 4 and 5 show the effect of the non-linear stretching parameter ( $n$ ) on the velocity and temperature profiles. Both profiles decrease with increasing ( $n$ ) in the nanofluids Copper-Water and Copper-Kerosene. However, due to membrane elongation and wall temperature, the speed and temperature of Copper-Water may be higher than Copper-Kerosene. Figure 6 shows the effect of the Prandtl number on the dimensionless temperature profile considering both the nanofluids. The mathematical description reveals that for the moderate retardation in the thermal diffusivity, the Prandtl number increases, which causes smooth retardation in the fluid temperature, i.e. a purely opposite value lowers the temperature of the fluid and, at the same time, lowers the thermal diffusivity. It is also worth noting that the temperature of Copper-Water is higher than that of Copper-Kerosene. Figures 7 and 8 are drawn for radiation parameters and Eckert numbers, respectively, for the fluid temperature distribution. It is interesting to note that and slowly increases the temperature profile, and in both cases, it was observed that the temperature of the Copper-water was higher than that of the Copper-Kerosene.

**Table 1.** Thermophysical Properties of Regular and Nano-fluids

	$c_p$ (J / KgK)	$\rho$ (Kg / m <sup>3</sup> )	$\kappa$ (W / mK)
<b>Water</b>	4179	997.1	613
<b>Cu</b>	385	8933	400
<b>Kerosene</b>	2090	783	0.145

**Table 2.** Validation of Nusselt number with Prandtl numbers

Pr	Khan and Pop [39]	Devi and Devi [40]	Present
2	0.9113	0.91135	0.9182732
6.13	----	1.75968	1.7563419
7	1.8954	1.8954	1.8973210
20	3.3539	3.3539	3.3501566

**Table 3.** Numerical Calculation of Rate Coefficients

$\phi$	$n$	Pr	Nr	Ec	$C_f$		Nu	
					Water-based	Kerosene based	Water-based	Kerosene based
0.1	0.5	7	0.1	0.5	-1.5155	-1.6154	5.7394	6.1014
0.2					-1.1705	-1.2763	6.6552	7.5322
0					-1.6792	-1.6792	4.9342	4.9342
0.1	1.5				-0.9837	-1.0485	3.5218	3.7438
	2				-1.7217	-1.8353	6.5759	6.9908
	0.5	0.71			-1.5155	-1.6154	1.9226	2.0391
		2			-1.5155	-1.6154	2.9795	3.1661
		7	0.2		-1.5155	-1.6154	6.5708	6.9848
			0.5		-1.5155	-1.6154	6.3329	6.7321
			0.1	0.1	-1.5155	-1.6154	5.7394	6.1014
				0.3	-1.5155	-1.6154	5.5612	5.9112

**Table 4.** t-Test for Rate Coefficients

	$C_f$		Nu	
	Water-based	Kerosene based	Water-based	Kerosene based
Mean	-1.46942	-1.55883	5.139355	5.4761
Variance	0.044779	0.045359	2.640415	3.179048
Observations	11	11	11	11
Pearson Correlation	0.988678		0.995563	
Hypothesized Mean Difference	0		0	
df	10		10	
t Stat	9.27407		-4.96054	
P(T<=t) one-tail	1.58E-06		0.000285	
t Critical one-tail	1.812461		1.812461	
P(T<=t) two-tail	3.16E-06		0.00057	
t Critical two-tail	2.228139		2.228139	

**Table 5.** Validation with previous studies

Authors	Year	Nanofluids	Nanoparticle	Model	Findings
Mohapatra et al. [17]	2019	Water and Kerosene	Copper	Maxwell model	Kerosene is denser in comparison to water, for which the velocity of Cu-water enhances than Cu-kerosene.
Tshivhi et al. [24]	2021	Water	Copper, Aluminium oxide, Iron Oxide	Maxwell model	Cu-water is a better coolant than the other two nanofluids, as this exhibits the highest heat transfer enhancement rate.
Mishra et al. [29]	2022	Water	Copper, Silver	Maxwell model	heat transfer rate rises for the involvement of copper nanoparticles in the dusty fluid, but the reverse result is an encounter for silver.
Pattnaik et al. [30]	2022	Water	Titanium dioxide	Tiwari-Das nanoscale model	The rate of heat transfer is enhanced.

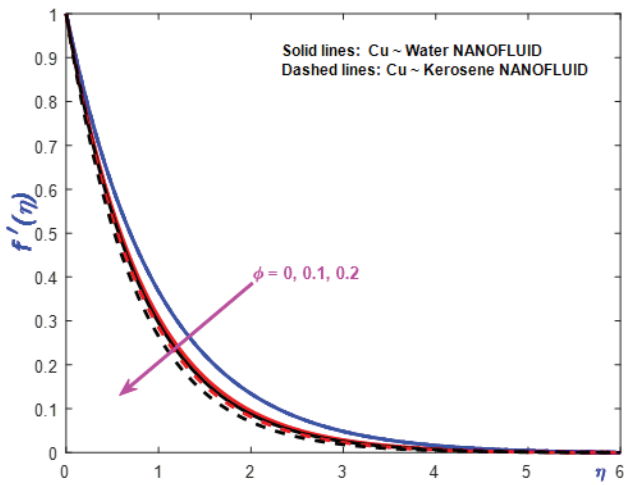


Figure 2. Influence of volume fraction parameter ( $\phi$ ) on velocity.

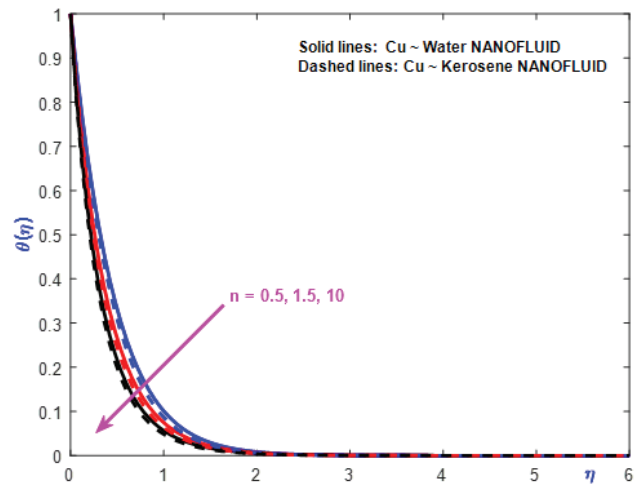


Figure 5. Influence of stretching parameter ( $n$ ) on temperature.

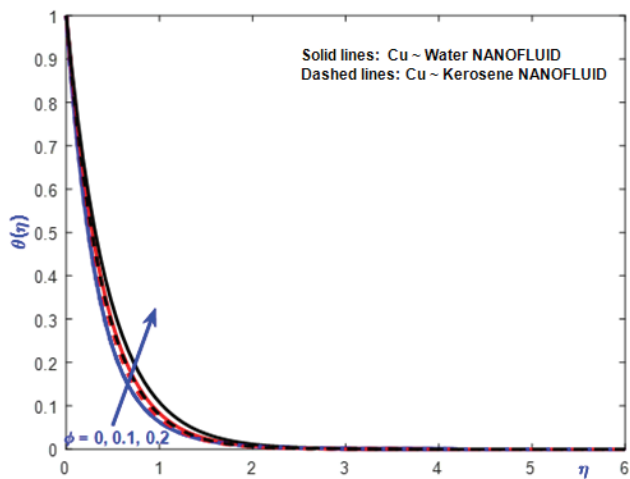


Figure 3. Influence of volume fraction parameter ( $\phi$ ) on temperature.

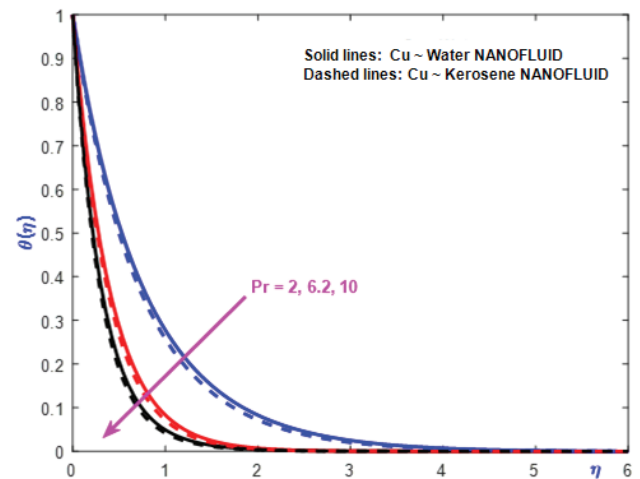


Figure 6. Influence of Prandtl number ( $Pr$ ) on temperature.

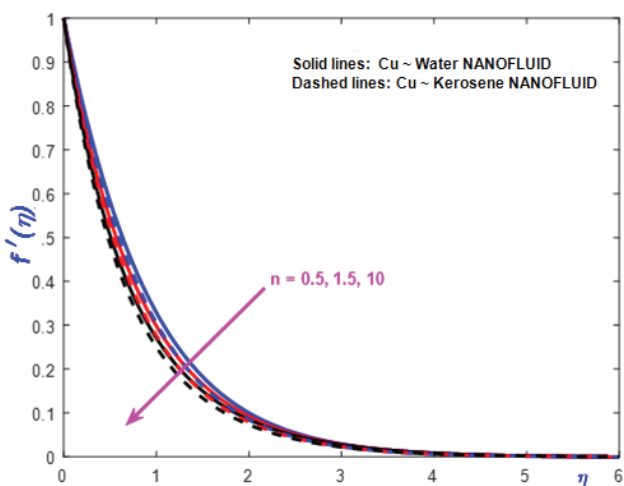


Figure 4. Influence of stretching parameter ( $n$ ) on velocity.

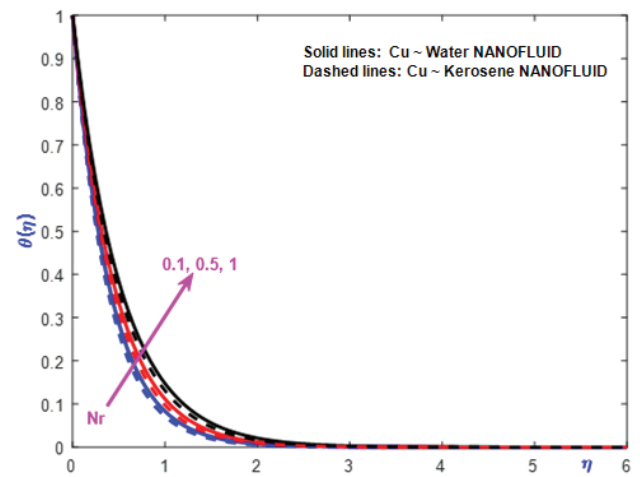


Figure 7. Influence of thermal radiation parameter ( $Nr$ ) on temperature.

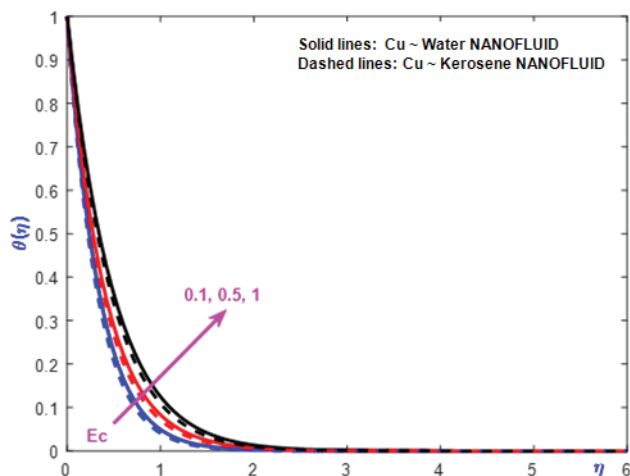


Figure 8. Influence of Eckert number ( $Ec$ ) on temperature.

### CONCLUSIONS

Simulated results for the flow of nanofluids in the presence of Cu nanoparticles over an expanding surface were carried out using water and kerosene-based liquids. On the other hand, the incorporation of thermal radiation and viscous dissipation encourages the occurrence of flow phenomena. The physical significance of the contributing parameters is depicted in graphs and tabular form to demonstrate their relationships. Furthermore, the following are the most significant observations made for both nanofluids:

- The comparative analysis in the particular case accumulated to the earlier study reveals a good correlation and also suggests the validation as well as the convergence criteria of the proposed methodology.
- The enhanced particle concentration, in conjunction with the nonlinear stretching parameter, retards the nanofluid velocity in either case of water and kerosene base fluids.
- The temperature profile becomes more pronounced for the enhanced radiation parameters, the solid volume fraction, and the Eckert number; however, the reverse trend is marked for the increasing Prandtl number and non-linear stretching parameter.
- Significant retardation in the shear rate coefficient is observed for the increasing particle concentration, whereas it overshoots the heat transfer rate.
- The combined effect of thermal radiation and the coupling parameter for the inclusion of dissipative heat, i.e. the augmented values of the Eckert number, decelerate the heat transfer rate.

Finally, but not least, Novelty of the current study not only illustrates the physical properties of the three defining parameters under specific conditions, but it also provides a roadmap for future research by incorporating the significant role of magnetic and electric fields in controlling fluid velocity, which will be beneficial for the manufacturing of

a variety of products in the industrial sector, among other things. Using different particle sizes, on the other hand, will greatly assist in producing a finished product that is precisely the right form and size. Another reason to use an analytical method for the suggested governing equations is that it will be easier to compare them in the future.

### NOMENCLATURE

$C$	constant
$C_f$	skin friction coefficient
$C_p$	specific heat capacity
$Ec$	Eckert number
$k$	thermal conductivity
$n$	nonlinear stretching parameter
$Nu$	Nusselt number
$Nr$	thermal radiation parameter
$Pr$	Prandtl number
$T_\infty$	ambient temperature
$\bar{T}_w$	wall temperature
$\bar{u}, \bar{v}$	velocity components along $x$ and $y$ directions
$\tilde{u}_w$	stretching velocity

#### Greek symbols

$\rho$	density
$\mu$	viscosity
$\phi$	solid volume fraction

#### Subscripts

$f$	base fluid
$s$	solid particle
$nf$	nanofluid

### AUTHORSHIP CONTRIBUTIONS

Authors equally contributed to this work.

### DATA AVAILABILITY STATEMENT

The authors confirm that the data that supports the findings of this study are available within the article. Raw data that support the finding of this study are available from the corresponding author, upon reasonable request.

### CONFLICT OF INTEREST

The author declared no potential conflicts of interest with respect to the research, authorship, and/or publication of this article.

### ETHICS

There are no ethical issues with the publication of this manuscript.

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